WELSH JOINT EDUCATION COMMITTEE General Certificate of Education Advanced Subsidiary/Advanced



CYD-BWYLLGOR ADDYSG CYMRU Tystysgrif Addysg Gyffredinol Uwch Gyfrannol/Uwch

973/01

MATHEMATICS C1

Pure Mathematics

A.M. MONDAY, 23 May 2005

 $(1\frac{1}{2} \text{ hours})$

NEW SPECIFICATION

ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- a 12 page answer book;
- a Formula Booklet.

INSTRUCTIONS TO CANDIDATES

Answer all questions.

Calculators are **not** allowed for this paper.

INFORMATION FOR CANDIDATES

The number of marks is given in brackets at the end of each question or part-question.

You are reminded of the necessity for good English and orderly presentation in your answers.

- 1. The points A, B, C, D have coordinates (1, 7), (5, -1), (8, 3), (6, 7) respectively.
 - (a) Show that AB and CD are parallel. [3]
 - (b) Find the equation of AB. [2]
 - (c) The line L passes through the point D and is perpendicular to AB. Show that L has equation

$$x - 2y + 8 = 0.$$
 [3]

- (d) The lines L and AB intersect at the point E. Find the coordinates of E. [2]
 (e) Calculate the length of EF, where F is the mid-point of AB. [4]
- 2. Simplify each of the following, expressing your answers in surd form:

(a)
$$\sqrt{45} + \sqrt{80} - \sqrt{125}$$
; [3]

(b)
$$\frac{6+\sqrt{2}}{2+\sqrt{2}}$$
. [4]

- 3. (a) Given that x 1 is a factor of $3x^3 + 5x^2 + ax 4$, show that a = -4. [2]
 - (b) Solve the equation $3x^3 + 5x^2 4x 4 = 0.$ [4]
 - (c) Calculate the remainder when $3x^3 + 5x^2 4x 4$ is divided by x + 1. [2]
- 4. Write down and simplify the first four terms in the binomial expansion of $(1 + 2x)^6$. [4]

5. Given
$$y = x^2 - 7x + 2$$
, find $\frac{dy}{dx}$ from first principles. [5]

6. The curve *C* has equation

$$y = 16\sqrt{x} + \frac{32}{x} + 2$$
 .

(a) Find the value of
$$\frac{dy}{dx}$$
 when $x = 4$. [3]

(b) Find the equation of the normal to C at the point where x = 4. [3]

- 7. The curve C has equation $y = x^3 3x^2$.
 - (a) Find the coordinates of the stationary points of *C* and determine the nature of each of these points. [7]
 - (b) Sketch C. [3]
 - (c) Find the range of values of k for which there are three real and distinct solutions of the equation $x^3 3x^2 = k$. [2]
- 8. (a) Express the quadratic expression $x^2 6x + 16$ in the form $(x a)^2 + b$, where the values of the constants a and b are to be determined. Deduce the least value of $x^2 6x + 16$.

[3]

(b) Solve the inequality

$$(x+1)^2 \leqslant 4x+9. \tag{4}$$

- 9. The straight line y = 2x + c is a tangent to the curve $y = x^2 + 6x + 7$.
 - (a) Determine the value of the constant c. [4]
 - (b) Find the coordinates of the point of contact of the tangent and the curve. [2]
- 10. The diagram shows the graph of y = f(x). The graph has a maximum point at (1, 3).



Sketch the following graphs, using a separate set of axes for each graph and indicating the coordinates of the stationary point in each case.

(a)
$$y = 4f(x)$$
 (b) $y = f(x-2)$ (c) $y = f\left(\frac{x}{2}\right)$ [2], [2], [2]

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