WELSH JOINT EDUCATION COMMITTEE General Certificate of Education Advanced Subsidiary/Advanced



CYD-BWYLLGOR ADDYSG CYMRU Tystysgrif Addysg Gyffredinol Uwch Gyfrannol/Uwch

974/01

MATHEMATICS C2

Pure Mathematics

A.M. MONDAY, 23 May 2005

 $(1\frac{1}{2} \text{ hours})$

NEW SPECIFICATION

ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- a 12 page answer book;
- a Formula Booklet;
- a calculator.

INSTRUCTIONS TO CANDIDATES

Answer all questions.

INFORMATION FOR CANDIDATES

The number of marks is given in brackets at the end of each question or part-question.

You are reminded of the necessity for good English and orderly presentation in your answers.

1. Use the Trapezium Rule with six ordinates to find an approximate value for

$$\int_0^1 \sqrt{1+x^2} \, \mathrm{d}x \; .$$

Show your working and give your answer correct to three decimal places.

2. (a) Find the values of x in the range $0 \le x \le 360^\circ$ satisfying

$$8\cos^2 x + 2\sin x - 7 = 0.$$
 [6]

(b) Find the values of x in the range $0^{\circ} \le x \le 180^{\circ}$ satisfying

$$\tan 2x = 1.$$
 [3]

[4]

3. (a) An arithmetic series has first term a and common difference d. Write down the nth term and prove that the sum of the first n terms is given by

$$S_n = \frac{n}{2} [2a + (n-1)d] .$$
 [4]

- (b) The seventh term of an arithmetic series is twice the third term. The sum of the first ten terms of the series is 195.
 - (i) Find the common difference of the series.
 - (ii) Find the sum of the first sixty terms. [7]
- 4. The sum of the first two terms of a geometric series is 6.4, and the sum to infinity of the series is 10.
 - (a) Given that the common ratio is positive, find its value. [5]
 - (b) Find, correct to three decimal places, the sum of the first eleven terms of the series. [3]
- 5. The circle C is given by the equation

$$x^2 + y^2 - 8x + 4y - 5 = 0.$$

- (a) Find the radius and the coordinates of the centre of C. [3]
- (b) (i) Show that P(1, -6) lies on C. [1]
 - (ii) Find the equation of the tangent to *C* at *P*. [4]

6. (a) Given that x > 0, y > 0, show that

$$\log_a\left(\frac{x}{y}\right) = \log_a x - \log_a y \quad [3]$$

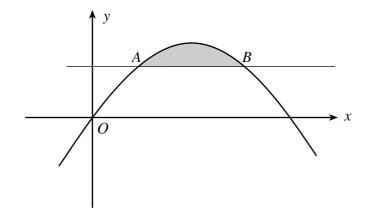
(b) (i) Solve the equation

$$5^{2x+1} = 7.$$

giving your answer correct to four decimal places.

(ii) Express $\log_{10} 2 + 2\log_{10} 18 - \frac{3}{2}\log_{10} 36$ as a single logarithm in its simplest form. [8]

7. (a) Find
$$\int \left(2x^{\frac{3}{4}} + \frac{7}{x^{\frac{1}{2}}}\right) dx$$
 [2]
(b)



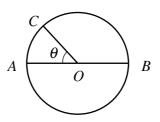
The diagram shows a sketch of the curve $y = 6x - x^2$ and the line y = 5. The line and the curve intersect at the points A and B.

- (i) Showing your working, find the coordinates of *A* and *B*.
- (ii) Find the area of the shaded region.

[10]

- 8. The triangle ABC is such that AB = x cm, BC = (x 3) cm, CA = (x 1) cm and $\overrightarrow{ABC} = 60^{\circ}$.
 - (a) Use the cosine rule to show that x = 8. [4]
 - (b) Find the area of triangle ABC, giving your answer in surd form. [2]

TURN OVER.



4

The diagram shows three points *A*, *B*, *C* on a circle with centre *O* and radius 4 cm, such that *AB* is a diameter of the circle and $AOC = \theta$ radians. Given that the area of the sector *BOC* is 5 cm² more than the area of the sector *AOC*,

(a) show that
$$\theta = \frac{8\pi - 5}{16}$$
, [3]

(b) calculate the difference between the arc length BC and the arc length AC. [3]