WELSH JOINT EDUCATION COMMITTEE General Certificate of Education Advanced Subsidiary/Advanced



CYD-BWYLLGOR ADDYSG CYMRU Tystysgrif Addysg Gyffredinol Uwch Gyfrannol/Uwch

### 983/01

### **MATHEMATICS S1**

## **Statistics**

P.M. WEDNESDAY, 18 January 2006

 $(1\frac{1}{2}$  hours)

# **NEW SPECIFICATION**

### **ADDITIONAL MATERIALS**

In addition to this examination paper, you will need:

- a 12 page answer book;
- a Formula Booklet;
- a calculator;
- statistical tables (Murdoch and Barnes or RND/WJEC Publications)

### **INSTRUCTIONS TO CANDIDATES**

Answer all questions.

#### **INFORMATION FOR CANDIDATES**

The number of marks is given in brackets at the end of each question or part-question.

You are reminded of the necessity for good English and orderly presentation in your answers.

1.	Two unbiased cubical dice are thrown simultaneously. Calculate the probability that

( <i>a</i> )	the score on each die is at least 3,	[	[3]
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- (b) the scores on the two dice differ by 3. [3]
- 2. The events A and B are such that P(A) = 0.5 and  $P(A \cup B) = 0.7$ . Determine the value of P(B) in each of the cases when
  - (a) A and B are mutually exclusive, [2]
    (b) A and B are independent, [4]
  - (c) P(B|A) = 0.3. [3]

**3.** The number of machine breakdowns, *X*, occurring in a certain factory in a randomly chosen week may be assumed to have a Poisson distribution with mean 4.

- (a) Write down the standard deviation of X. [1]
- (b) Find the probability that the number of machine breakdowns in a randomly chosen week is
  - (i) exactly 3,(ii) between 2 and 6 (both inclusive). [5]
- (c) The cost C (in appropriate monetary units) of repairing these machines is given by

$$C = 5 + 4X.$$

Find the mean and standard deviation of *C*. [4]

**4.** A bag contains 5 red balls and 3 blue balls. A random sample of 3 balls is selected from the bag, without replacement. Calculate the probability that

( <i>a</i> )	all the selected balls are red,	[2]
(b)	more blue balls are selected than red balls.	[4]

- 5. The random variable *X* has the binomial distribution B(n,p). The mean and standard deviation of *X* are 20 and 4 respectively. Find the values of *n* and *p*. [6]
- 6. Jim has a fair cubical die with the six faces numbered 1, 2, 3, 4, 5, 6 respectively and a fair tetrahedral die with the four faces numbered 1, 2, 3, 4 respectively. He tosses a fair coin. If it falls 'heads', he throws the cubical die. If it falls 'heads', he throws the tetrahedral die.
  - (a) Calculate the probability that he obtains a '4'. [3]
  - (b) Given that he obtains a '4', find the probability that he threw the cubical die. [3]

- 7. Wine glasses are mass produced. There is a probability of 0.05 that a randomly selected glass is defective, independently of all other glasses.
  - (a) Without using tables, find the probability that a set of 24 glasses contains exactly 2 defective glasses.
  - (b) Using tables, find the probability that a set of 50 glasses contains between 3 and 5 (both inclusive) defective glasses. [3]
  - (c) Use a Poisson approximation to find the probability that a set of 120 glasses contains fewer than 8 defective glasses.
- 8. The following table gives the probability distribution of the discrete random variable X, where  $\theta$  is a constant.

x	1	2	3	4
P(X = x)	0.1	0.2	θ	$0.7 - \theta$

- (a) State the range of possible values of  $\theta$ .
- (b) Given that E(X) = 3,
  - (i) find the value of  $\theta$ ,
  - (ii) evaluate  $E(X^3)$ .
- 9. The continuous random variable X has probability density function f given by

$f(x) = kx^2$	for $1 \leq x \leq 4$ ,
f(x) = 0	otherwise,

where k is a constant.

$$k = \frac{1}{21}.$$

(ii) Evaluate E(X).

- (b) (i) Obtain an expression for F(x), valid for  $1 \le x \le 4$ , where *F* denotes the cumulative distribution function of *X*.
  - (ii) Evaluate  $P(2 \le X \le 3)$ .
  - (iii) Find the median of X.

[2]

[7]

[6]

[8]