WELSH JOINT EDUCATION COMMITTEE General Certificate of Education Advanced Subsidiary/Advanced



CYD-BWYLLGOR ADDYSG CYMRU Tystysgrif Addysg Gyffredinol Uwch Gyfrannol/Uwch

984/01

MATHEMATICS S2

STATISTICS 2

P.M. MONDAY, 11 June 2007

 $(1\frac{1}{2} \text{ hours})$

ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- a 12 page answer book;
- a Formula Booklet;
- a calculator;
- statistical tables (Murdoch and Barnes or RND/WJEC Publications)

INSTRUCTIONS TO CANDIDATES

Answer all questions.

INFORMATION FOR CANDIDATES

The number of marks is given in brackets at the end of each question or part-question. You are reminded of the necessity for good English and orderly presentation in your answers. 1. The weights, in kg, of babies born during a particular week in a hospital are given below.

3.25 3.38 3.04 3.59 3.42 3.13 3.38 3.09 3.15

- (a) Assuming that this is a random sample from a normal distribution with mean μ and standard deviation 0.15, calculate a 90% confidence interval for μ . [5]
- (b) How many observations would be required to halve the width of this 90% confidence interval? [2]
- 2. The independent random variables X and Y are Poisson distributed with means 2 and 3 respectively.
 - (a) (i) Show that $E(X^2) = 6$ and evaluate $E(Y^2)$.

(ii) Deduce the value of
$$E(X^2Y^2)$$
. [5]

[4]

(b) The random variable U is defined by

$$U = XY.$$

Determine the standard deviation of U.

- **3.** The weights of apples may be assumed to be normally distributed with mean 75 grams and standard deviation 5 grams.
 - (a) (i) Find the probability that a randomly chosen apple weighs less than 80 grams.
 - (ii) Find the upper quartile of the weights of apples. [6]
 - (b) The weights of plums may be assumed to be normally distributed with mean 56 grams and standard deviation 4 grams. Calculate the probability that the combined weight of 3 plums exceeds the combined weight of 2 apples.
- 4. A circle has radius R cm, where R is a continuous random variable that is uniformly distributed on the interval [0, 5].
 - (a) State the probability density function of R. [1]
 - (b) Find the expected area of the circle. [4]
 - (c) Find the probability that the area of the circle is greater than 25 cm², giving your answer correct to three decimal places. [4]

- 5. Jim is a darts player. When he throws a dart, he claims to be able to hit the 'bull' with probability 0.75. His friends believe that the probability is less than this.
 - (a) State suitable hypotheses to test Jim's claim.
 - (b) They decide to set up a trial in which Jim throws 20 darts and they define X to be the number of darts hitting the 'bull'.
 - (i) Taking the critical region to be $X \le k$, find the value of k for which the significance level is nearest to 10%.
 - (ii) The actual value of the probability of Jim hitting the 'bull' is 0.5. With the value of k found in (i), find the probability of reaching an incorrect conclusion. [7]
- 6. A plumber knows that the number of emergency calls received per day follows a Poisson distribution with mean $\mu = 2$.
 - (a) Calculate the probability that, in a 7-day period, he receives
 - (i) exactly 10 calls,
 - (ii) more than 12 calls.

[5]

[1]

- (b) Wishing to increase the value of μ , he increases his advertising budget.
 - (i) State suitable hypotheses for investigating whether or not this achieves the desired result.
 - (ii) In the first 7-day period after increasing the budget, he receives 20 emergency calls. Calculate and interpret the *p*-value of this result.
 - (iii) In the next 100-day period, he receives 230 emergency calls. Calculate an approximate *p*-value of this result and interpret it. [12]
- 7. A scientist wishes to determine whether or not there is a difference in the acidity levels of two different liquids. He therefore makes five independent measurements of the acidity level of each liquid with the following results.

Liquid 1	6.31	6.38	6.33	6.34	6.35
Liquid 2	6.28	6.31	6.29	6.35	6.30

You may assume that these are random samples from normal distributions with common standard deviation 0.025.

- (a) (i) State suitable hypotheses.
 - (ii) Calculate the *p*-value of the above measurements and interpret your value in context.

[10]

(b) Find a 95% confidence interval for the difference in the acidity levels of the two liquids. [3]